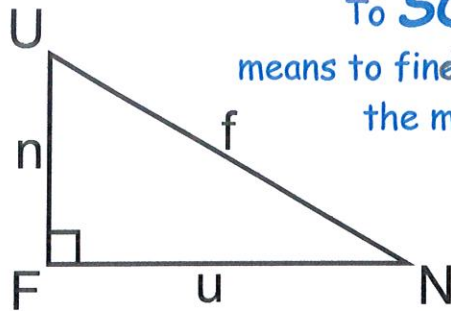


## Solving Right Triangles

To **SOLVE A TRIANGLE**

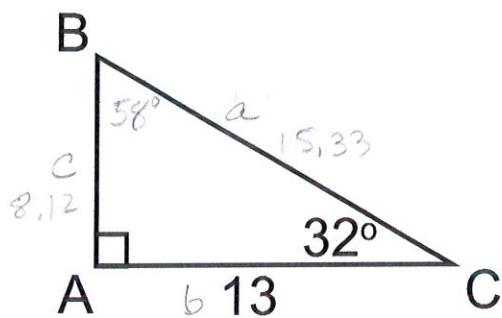
means to find the lengths of all missing sides and the measures of all missing angles.



To **SOLVE A RIGHT TRIANGLE** use:

- \* the sum of the angles in a triangle is  $180^\circ$
- \* Trig Ratios - SOH CAH TOA (preferred)
- \* Pythagorean Theorem (for checking ONLY!)

### Example 1:



$$A = 90^\circ \quad a = 15.33$$

$$B = 58^\circ \quad b = 13$$

$$C = 32^\circ \quad c = 8.12$$

Side c

$$(13) \tan 32 = \frac{c}{13} \quad (13)$$

$$13 \tan 32 = c$$

$$\boxed{8.12 = c}$$

Side a

$$8.12^2 + 13^2 = a^2$$

$$234.93 = a^2$$

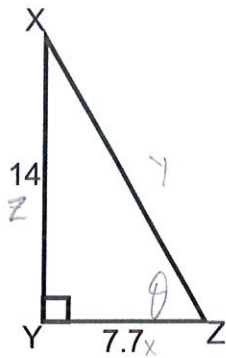
$$\boxed{15.33 = a}$$

Angle B

$$180 - 90 - 32$$

$$\boxed{= 58^\circ}$$

**Example 2:**



$X = 28.81^\circ$     $x = 7.7$   
 $Y = 90^\circ$     $y = 15.98$   
 $Z = 61.19^\circ$     $z = 14$

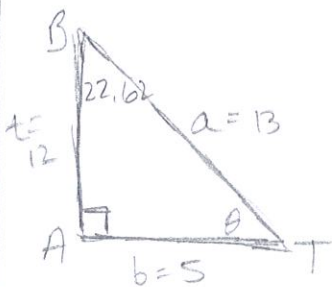
Angle Z  
 $\tan \theta = \frac{14}{7.7}$   
 $\theta = \tan^{-1} \frac{14}{7.7}$   
 $\theta = 61.19^\circ$

Angle X  
 $90 - 61.19$   
 $= 28.81^\circ$

Side y  
 $14^2 + 7.7^2 = y^2$   
 $255.29 = y^2$   
 $15.98 = y$

**Example 3:**

Solve triangle BAT given that angle A is the right angle, side b = 5 and side t = 12.



$B = 22.62^\circ$     $b = 5$   
 $A = 90^\circ$     $a = 13$   
 $T = 67.38^\circ$     $t = 12$

Angle T  
 $\tan \theta = \frac{12}{5}$   
 $\theta = \tan^{-1} \frac{12}{5}$   
 $\theta = 67.38^\circ$

Angle B  
 $90 - 67.38$   
 $= 22.62^\circ$

Side a  
 $12^2 + 5^2 = a^2$   
 $144 + 25 = a^2$   
 $13 = a$