

Warmup 9: Use the sum or difference formula
to find the exact value of $\sin \frac{13\pi}{12} = \frac{3\pi}{12} + \frac{10\pi}{12}$

$$\sin \frac{13\pi}{12} = \sin \left(\frac{\pi}{4} + \frac{5\pi}{6} \right)$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$= \sin \frac{\pi}{4} \cos \frac{5\pi}{6} + \cos \frac{\pi}{4} \sin \frac{5\pi}{6}$$

$$= \frac{\sqrt{2}}{2} \cdot \frac{-\sqrt{3}}{2} + \frac{\sqrt{2}}{2} \cdot \frac{1}{2}$$

$$= \frac{-\sqrt{6}}{4} + \frac{\sqrt{2}}{4}$$

$$= \boxed{\frac{-\sqrt{6} + \sqrt{2}}{4}} \text{ or } \boxed{\frac{\sqrt{2} - \sqrt{6}}{4}}$$